

$$\sqrt{80} = 4\sqrt{5}$$

why ???

$$\frac{2}{4} = \frac{1}{2}$$

... you always reduce fractions right?  
 ... well we do the same for radicals.

$$80 = 2 \cdot 40$$

$$80 = 4 \cdot 20$$

$$80 = 16 \cdot 5$$

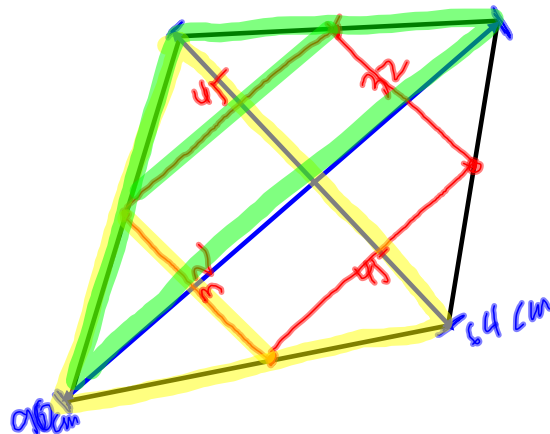
largest perfect square factor

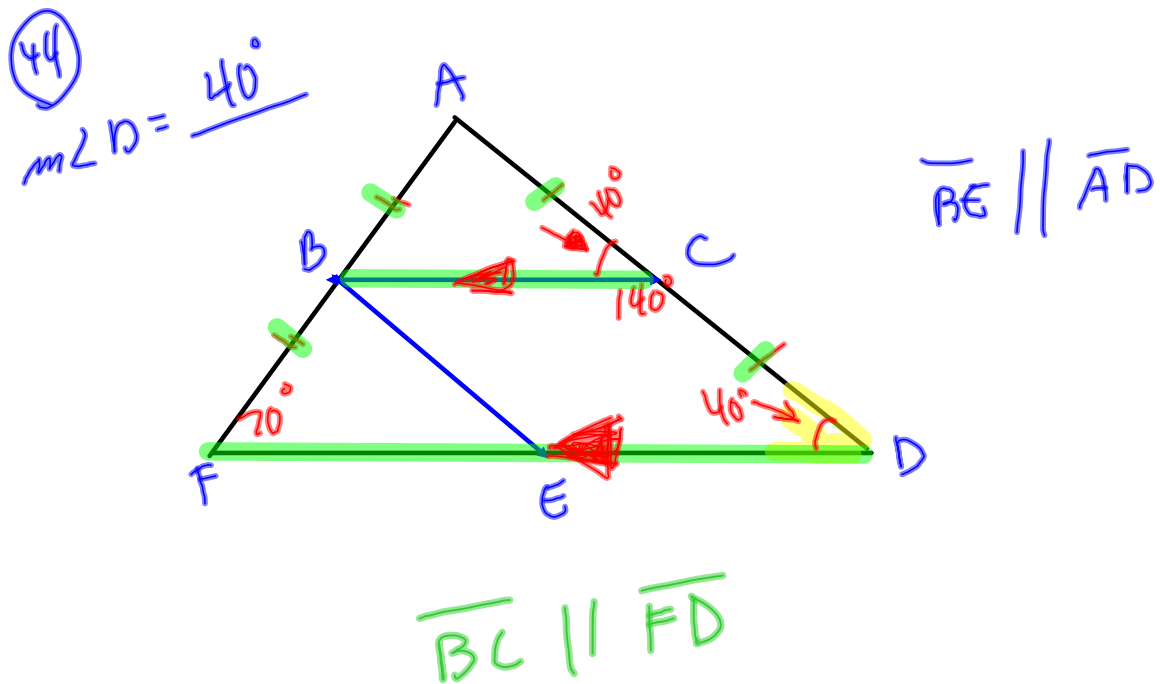
$$\sqrt{80} = \sqrt{16 \cdot 5} = \sqrt{16} \cdot \sqrt{5} = 4 \cdot \sqrt{5} = 4\sqrt{5}$$

simplest radical form

perfect squares: 4, 9, 16, 25, 36, 49, 64, 81, ...  
 $\div 80$ ?

(33)





### Construct a Perpendicular Bisector to a Segment

- 1) Using a straight edge, draw a segment on your paper.
- 2) Using your compass, construct its perpendicular bisector.

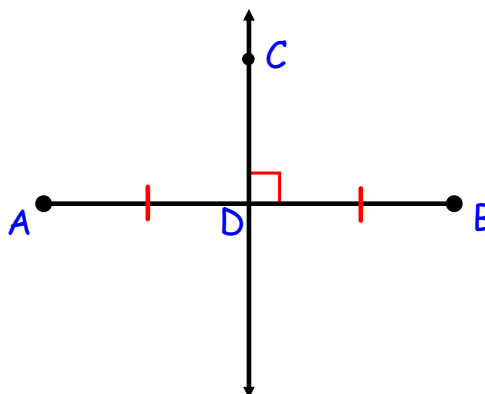
### Construct an Angle Bisector

- 1) Using a straight edge, draw an angle on your paper.
- 2) Using your compass, construct its bisector.

Theorem 5-2: Perpendicular Bisector Theorem

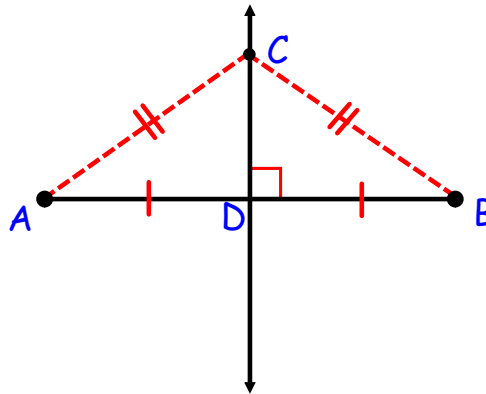
Theorem 5-2: Perpendicular Bisector Theorem

If a pt is on  $\perp$  bisector of a seg.



## Theorem 5-2: Perpendicular Bisector Theorem

If a pt is on  $\perp$  bisector of a seg.  
then it is equidist from endpts of the seg.



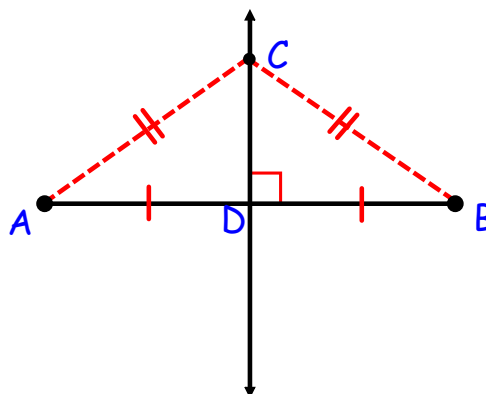
## Theorem 5-2: Perpendicular Bisector Theorem

If a pt is on  $\perp$  bisector of a seg.  
then it is equidist from endpts of the seg.

Given:  $\overleftrightarrow{CD} \perp \overline{AB}$

$\overleftrightarrow{CD}$  bisects  $\overline{AB}$

Then:  $\overline{CA} \cong \overline{CB}$



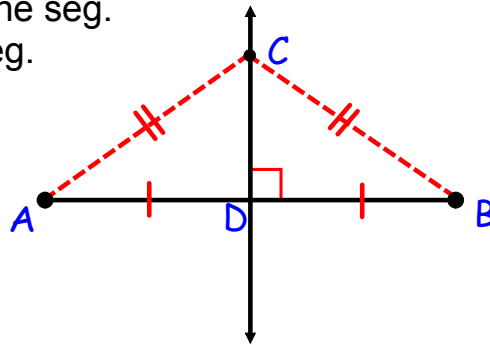
### Theorem 5-3: Conv of Perpendicular Bisector Theorem

If a pt is equidist from endpts of the seg.  
Then it is on  $\perp$  bisector of that seg.

Given:  $\overline{CA} \cong \overline{CB}$

Then:  $\overleftrightarrow{CD} \perp \overline{AB}$

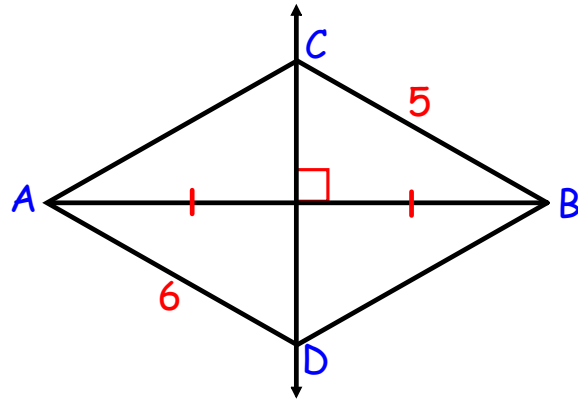
$\overleftrightarrow{CD}$  bisects  $\overline{AB}$



Questions

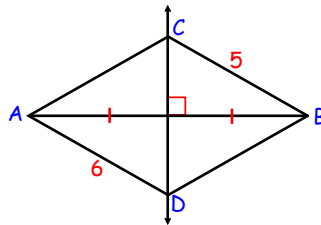
Next...

1 CA =



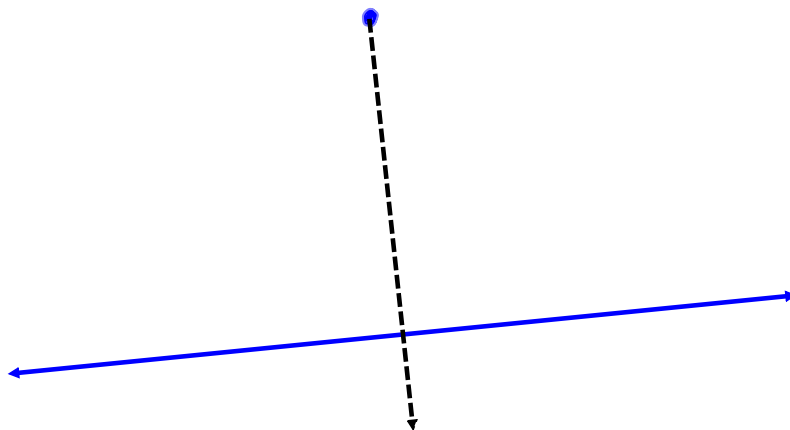
1) CA = ?

2) DB = ?



back...

Defn: Distance from a pt to a line



Defn: Distance from a pt to a line

The dist from a pt to a line

Defn: Distance from a pt to a line

The dist from a pt to a line

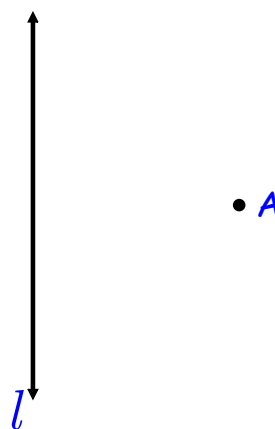
is the len of  $\perp$  seg from pt to line.

Defn: Distance from a pt to a line

The dist from a pt to a line

is the len of  $\perp$  seg from pt to line.

dist fm pt  $A$  to line  $l =$



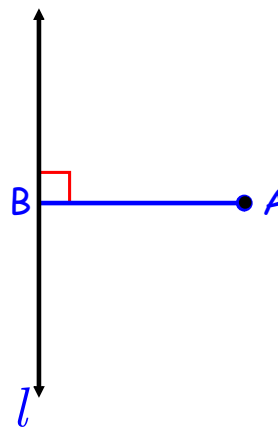


Defn: Distance from a pt to a line

The dist from a pt to a line

is the len of  $\perp$  seg from pt to line.

dist fm pt  $A$  to line  $l = AB$



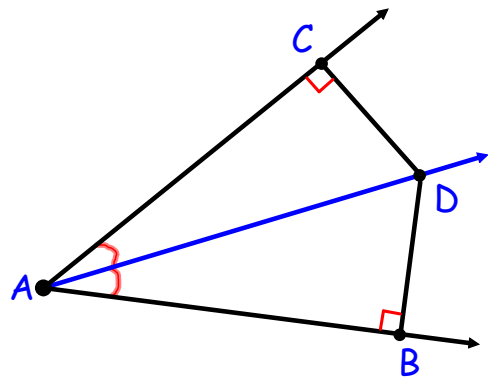
Theorem 5-4: Angle Bisector Theorem

### Theorem 5-4: Angle Bisector Theorem

If a pt is on an  $\angle$  bisector  
then it is equidist from sides of the  $\angle$ .

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### Theorem 5-4: Angle Bisector Theorem

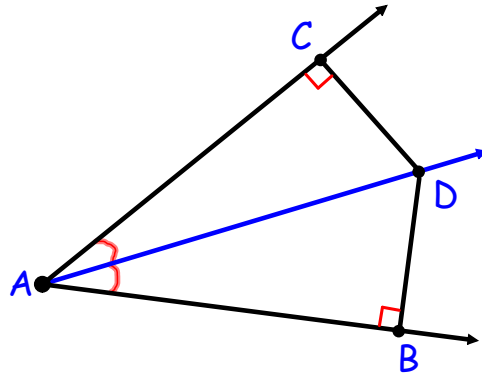
If a pt is on an  $\angle$  bisector  
then it is equidist from sides of the  $\angle$ .

Given:  $\overrightarrow{AD}$  bisects  $\angle CAB$

$$\overline{CD} \perp \overline{AC}$$

$$\overline{BD} \perp \overline{AB}$$

Prove:  $CD = BD$



### Theorem 5-4: Angle Bisector Theorem

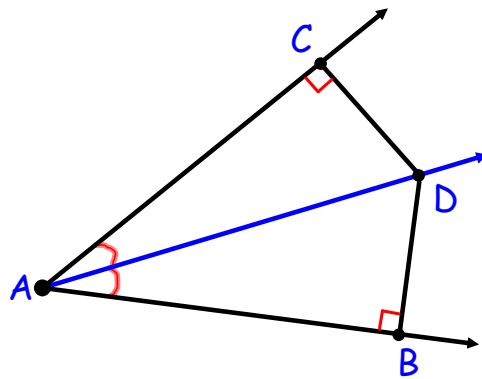
If a pt is on an  $\angle$  bisector  
then it is equidist from sides of the  $\angle$ .

Given:  $\overrightarrow{AD}$  bisects  $\angle CAB$

$$\overline{CD} \perp \overline{AC}$$

$$\overline{BD} \perp \overline{AB}$$

Prove:  $CD = BD$



$$\angle CAD \cong \angle BAD \quad \text{defn } \angle \text{ bisector}$$

### Theorem 5-4: Angle Bisector Theorem

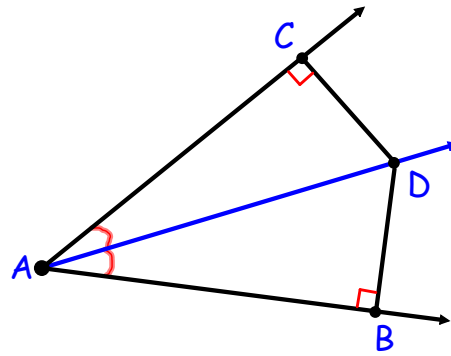
If a pt is on an  $\angle$  bisector  
then it is equidist from sides of the  $\angle$ .

Given:  $\overrightarrow{AD}$  bisects  $\angle CAB$

$$\begin{aligned} \overline{CD} &\perp \overline{AC} \\ \overline{BD} &\perp \overline{AB} \end{aligned}$$

Prove:  $CD = BD$

$$\begin{aligned} \angle CAD &\cong \angle BAD && \text{defn } \angle \text{ bisector} \\ \angle ACD &\cong \angle ABD && \text{all rt } \angle \text{'s } \cong \end{aligned}$$



### Theorem 5-4: Angle Bisector Theorem

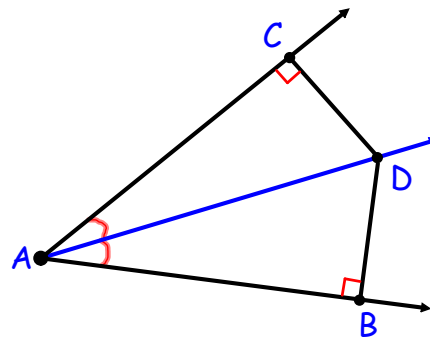
If a pt is on an  $\angle$  bisector  
then it is equidist from sides of the  $\angle$ .

Given:  $\overrightarrow{AD}$  bisects  $\angle CAB$

$$\begin{aligned} \overline{CD} &\perp \overline{AC} \\ \overline{BD} &\perp \overline{AB} \end{aligned}$$

Prove:  $CD = BD$

$$\begin{aligned} \angle CAD &\cong \angle BAD && \text{defn } \angle \text{ bisector} \\ \angle ACD &\cong \angle ABD && \text{all rt } \angle \text{'s } \cong \\ \overline{AD} &\cong \overline{AD} && \text{reflex POC} \end{aligned}$$



**Theorem 5-4: Angle Bisector Theorem**

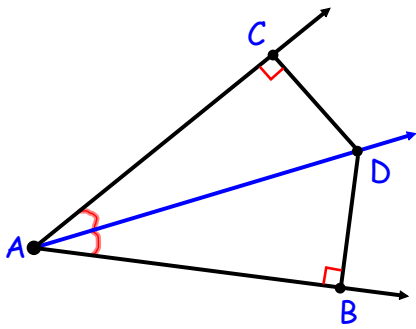
If a pt is on an  $\angle$  bisector  
then it is equidist from sides of the  $\angle$ .

Given:  $\overrightarrow{AD}$  bisects  $\angle CAB$

$$\overline{CD} \perp \overline{AC}$$

$$\overline{BD} \perp \overline{AB}$$

Prove:  $CD = BD$



- $\angle CAD \cong \angle BAD$     *defn  $\angle$  bisector*
- $\angle ACD \cong \angle ABD$     *all rt  $\angle$ 's  $\cong$*
- $\overline{AD} \cong \overline{AD}$         *reflex POC*
- $\triangle CAD \cong \triangle BAD$     *AAS*

**Theorem 5-4: Angle Bisector Theorem**

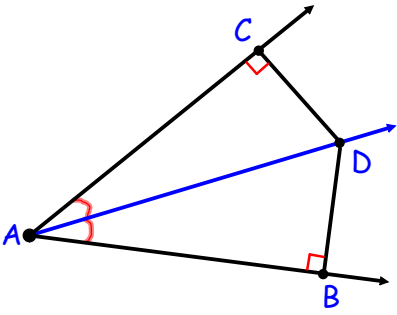
If a pt is on an  $\angle$  bisector  
then it is equidist from sides of the  $\angle$ .

Given:  $\overrightarrow{AD}$  bisects  $\angle CAB$

$$\overline{CD} \perp \overline{AC}$$

$$\overline{BD} \perp \overline{AB}$$

Prove:  $CD = BD$



- $\angle CAD \cong \angle BAD$     *defn  $\angle$  bisector*
- $\angle ACD \cong \angle ABD$     *all rt  $\angle$ 's  $\cong$*
- $\overline{AD} \cong \overline{AD}$         *reflex POC*
- $\triangle CAD \cong \triangle BAD$     *AAS*
- $\overline{CD} \cong \overline{BD}$         *CPCTC*

### Theorem 5-4: Angle Bisector Theorem

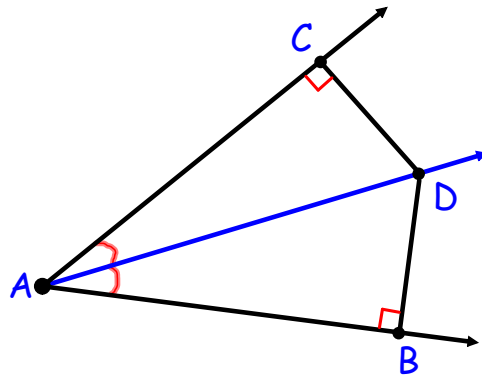
If a pt is on an  $\angle$  bisector  
then it is equidist from sides of the  $\angle$ .

Given:  $\overrightarrow{AD}$  bisects  $\angle CAB$

$$\overline{CD} \perp \overline{AC}$$

$$\overline{BD} \perp \overline{AB}$$

Prove:  $CD = BD$



$$\angle CAD \cong \angle BAD \quad \text{defn } \angle \text{ bisector}$$

$$\angle ACD \cong \angle ABD \quad \text{all rt } \angle \text{'s } \cong$$

$$\overline{AD} \cong \overline{AD} \quad \text{reflex POC}$$

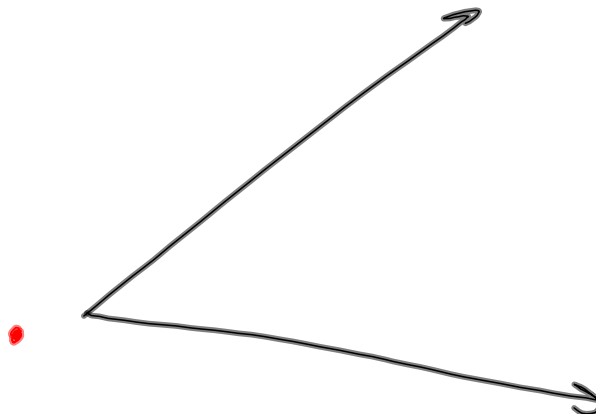
$$\triangle CAD \cong \triangle BAD \quad \text{AAS}$$

$$\overline{CD} \cong \overline{BD} \quad \text{CPCTC}$$

**QED**

### Theorem 5-5: Converse of Angle Bisector Theorem

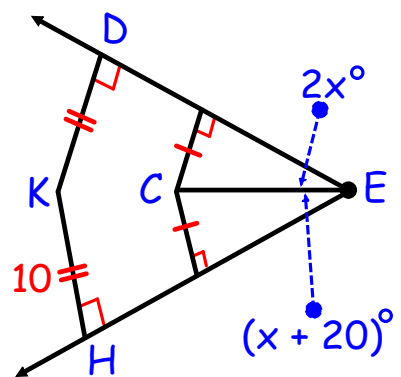
If a pt in **the interior** of an  $\angle$  is equidist from sides of the  $\angle$   
then it is on the  $\angle$  bisector.



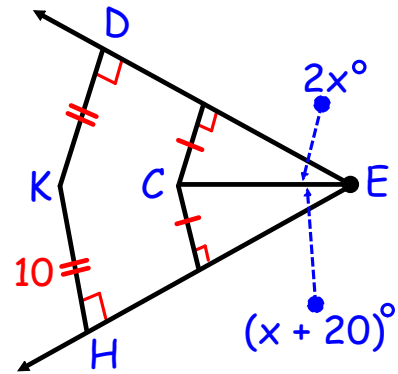
Questions

Next...

1  $KD = ?$



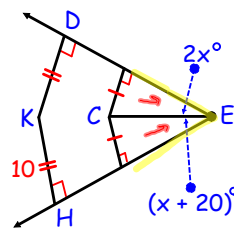
2  $x = ?$



1)  $KD = ?$

2)  $x = ?$  *20*

3)  $m\angle DEH = ?$   *$2x + (x + 20)$   
 $40 + 40$   
 $80$*



back...



L5-2 HW Problems

Pg 251 #1-25,  
35-39 odd,  
44, 46, 50-52